



Article

Optimisation and management of energy generated by a multifunctional MFC-integrated composite chassis for rail vehicles

Yiding Liu ¹, Sijun Du ², Christopher Micallef ¹, Yu Jia ^{3,4,*}, Yu Shi ^{4,*}, and Darren J. Hughes ^{1,*}¹ Warwick Manufacturing Group, University of Warwick, Coventry CV4 7AL, UK;Yiding.liu@warwick.ac.uk (Y.L.); Christopher.Micallef@warwick.ac.uk (C.M.)² Department of Electrical Engineering and Computer Sciences, University of California at Berkeley, Berkeley CA 94720, USA; sijun@berkeley.edu (S.D.)³ School of Engineering and Applied Science, Aston University, Birmingham B4 7ET, UK;⁴ Department of Mechanical Engineering, University of Chester, Chester CH2 4NU, UK;* Correspondence: yu.jia.gb@ieee.org (Y.J.); y.shi@chester.ac.uk (Y.S.); D.hughes@warwick.ac.uk (D.H.)

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Abstract: With the advancing trend towards lighter and faster rail transport, there is an increasing interest to integrate composite and advanced multifunctional materials in order to infuse smart sensing and monitoring, energy harvesting and wireless capabilities within the otherwise purely mechanical rail structures and the infrastructure. This paper presents a holistic multiphysics numerical study, across both mechanical and electrical domains, that describes an innovative technique of harvesting energy from a piezoelectric micro fibre composites (MFC) built-in composite rail chassis structure. Representative environmental vibration data measured from a rail cabin has been critically leveraged here to help predict the actual vibratory and power output behaviour under service. Time domain mean stress distribution data from the Finite Element simulation was used to predict the raw AC voltage output of the MFCs. Conditioned power output was then calculated using circuit simulation of several state-of-the-art power conditioning circuits. A peak instantaneous rectified power of 181.9 mW was obtained when an eight-stage Synchronised Switch Harvesting Capacitors (SSHC) from eight embedded MFCs located. The results showed that the harvested energy could be sufficient to sustain a self-powered structural health monitoring system with wireless communication capabilities. This study serves as a theoretical foundation of scavenging of vibrational power from the ambient state in a rail environment as well as to pointing to design principles to develop regenerative and power neutral smart vehicles.

Keywords: vibration energy harvesting; micro fibre composite; finite element analysis; circuit design and optimization; power conditioning circuit; lightweight rail vehicle

1. Introduction

Rail transport, as a means of transit for passengers and goods in daily life, is now increasingly targeting and transforming towards lightweight, faster speeds and net zero carbon emissions. The current state-of-the-art in the automotive sector suggests to use “right material in the right place” to satisfy the stiffness, strength and crashworthiness certification requirements. This leads to the application of composite materials, such as carbon fibre or glass fibre reinforced polymers due to their lighter weight and high stiffness-to-weight ratio. Subsequently, particularly in light of the global energy crisis and environment concerns, smart composites with energy harvesting capabilities have developed into an attractive research frontier [1]. Vibrations exists throughout the rail transportation system, such as the vibration of floor and vehicle chassis, railway train or tracks, etc. and hence it could offer an alternative energy source to compensate for the dissipation of kinetic energy during

vehicle vibration and motion [2].

Vibration-based energy harvesting, as one of the most promising research fields, has been established utilising electromagnetic generators [3], piezoelectric generators [4,5], MEMS-scale electrostatic generators [6], triboelectric [7,8] and magnetostrictive effects [9]. Figure 1 illustrates the means of energy harvesting mechanisms and their application possibilities to the railway industry, adopted from [10–15]. However, the application of different energy harvesting systems depends on the specific requirements, i.e. environmental conditions and physical constraints [16]. Electromagnetic inductions produce energy harvesting by means of permanent magnets, a coil and a resonating cantilever beam, however, magnets also add to the inertial mass [17]. Electrostatic generators require an initial constant polarisation of voltage field or charge. When using electrets to provide the initial charge, the output impedance is often quite high which makes them less suitable as a power supply [17]. Among them, piezoelectric materials offer great benefit to convert mechanical energy into electric energy due to their relatively high energy density and scalability [16,18]. As conventional piezoelectric ceramics are brittle and easily broken, the macro-fibre composite (MFC) can be used as energy harvesting device due to its structural flexibility, high efficiency and almost negligible thickness, which has been successfully developed by Shi's work investigating their application into an aircraft's wing structure [19] and Yuan's work on a one tenth scale experimental rig of a urban rail vehicle [20].

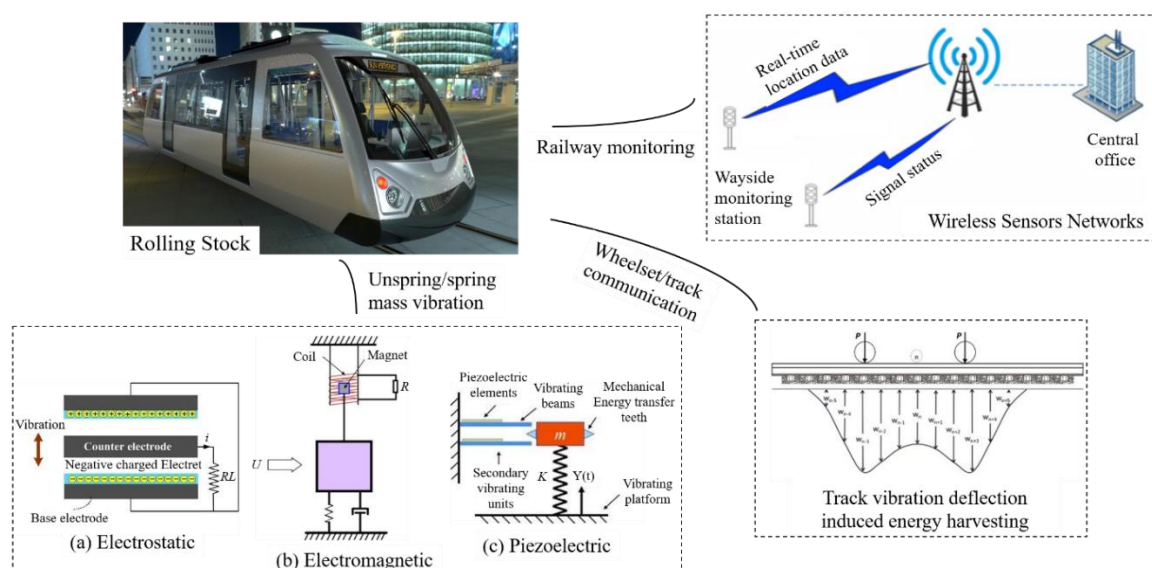


Figure 1. Illustration of energy harvesting applied to the railway industry, adopted from [10–15].

With respect to energy harvesting specific for railway application, most studies have focused on the vehicle brakes, shock absorbers, and exhaust systems and rail/track interfaces. Numerous research endeavours have been extended to investigate the energy harvesting potential from railway tracks as the tracks sustain the full load of the vehicle when the train moves [1]. Zuo et al. [1] stated that the actual harvested power from railway tracks depends on the speed of the train, the weight of the train and the type of railway track. For instance, for a four-wheel railcar of 100 tonnes at a speed of 40 miles/h, the average power potential is about 2 kW under 6.35 mm track deflection according to analytical analysis. This amount of power is sufficient for most of the trackside electric facilities, e.g. typically the light-emitting diode (LED) signal lights require a power of 8–10 W and level-crossing gates require a power of 150–200 W [1]. Pourghodrat et al. [21] proposed a hydraulic energy harvesting system to harness power from both downward and upward deflections of the track. The system could provide an average power of 1.9 W under a deflection of 2.8 mm and maximum load of 6.4 t. Hadas et al. [22] developed a model-based design of various harvesting systems embedded inside track sleepers and the maximum predicted harvested power was around 2 W during train passing at speed.

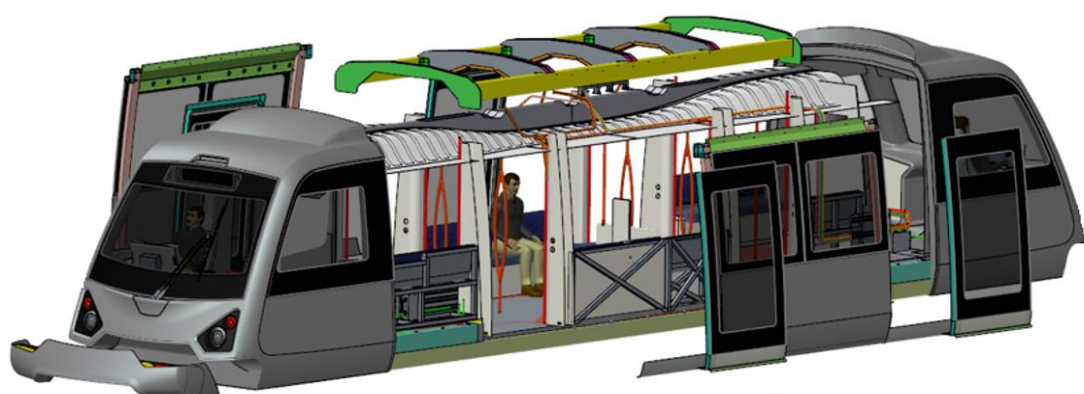
The works above discussed comparably in large-scale energy harvesting at 1 W to 100 kW which

promised a solution for self-powering the active devices, such as energy recovery from a suspension [2]. However, a fundamental challenge is that such large-scale vibrations are rarely maintained at time-varying frequency and at alternating velocities, resulting in the energy harvested unsustainable, inefficient and eventually unreliable for powering functional devices. However, small-scale vibrations are too difficult to avoid during service of rail vehicles and ideally meeting the energy request under sustainable supplying if they could be efficiently harvested. Hence, the balance of combined vibration control and efficiency of energy harvesting could be a critical concern considered for small-scale vibration harvesting. So far, the most micro-scale harvested power ranging from 10 μ W to 100 mW was significantly ignored in the railway industry, especially the vibrations from the vehicle structures when running on the individual routes and therefore wasted. However, such energy could be the important source for self-powering the wireless sensors and low-power electronics, which effectively resolves the difficulties of connections by wires/cables during assembly and induced extra weight. The current study is focusing on these micro-scale powers harvested from the composite chassis of rail vehicle under a low frequency operational vibration. Considering the power requirement of sensing and wireless sensor nodes for communication [23], the optimisation and energy management during harvesting process is numerically predicted for the real-world implementations of rail sectors based on our previous works presented in [24] and [25].

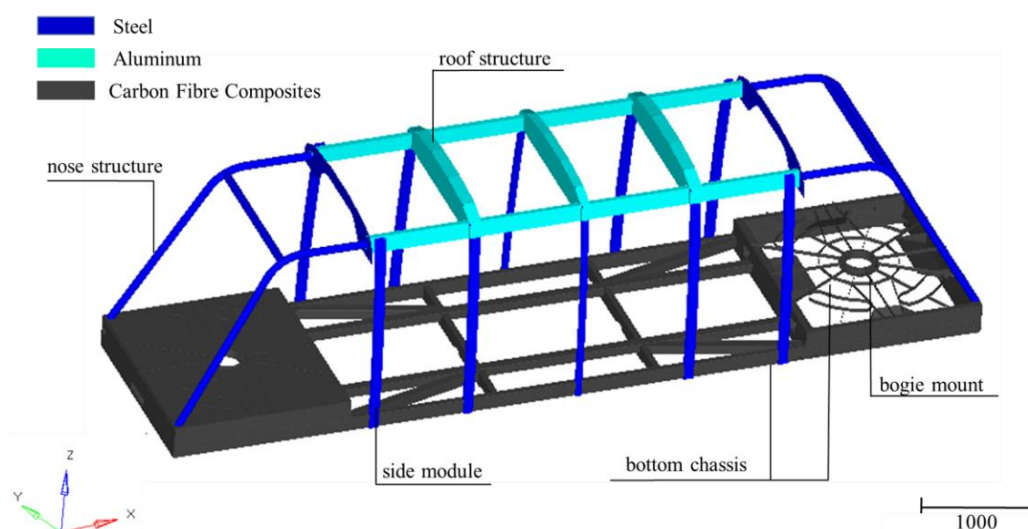
Most existing piezoelectric models are either based on analytical analysis (based on beam theory) [16,26–28] or experimental tests [20–22]. Analytical models are beneficial in understanding the underlying physics, however, it is difficult to simplify the complicated geometries. Experimental evaluations are useful to provide situations that are more realistic, however, they are time and cost consuming and the results are highly subjective due to the possibility of human error. On the other hand, finite element (FE) models can support complex assemblies while including multi-physical modules. Jia and Shi et al. [28] proposed using an FE model to simulate the electrical and mechanical behaviour of an integrated MFC on a carbon fibre composite beam using COMSOL Multiphysics combining solid mechanics, electrostatic and electrical-circuit-physics models. It has specific requirement on the computer hardware if applied to a large complex geometry including multi modules.

This work specifically relates to an industrial challenged project at Warwick Manufacturing Group (WMG), the University of Warwick, where a new class of lightweight rail vehicle is in development for upgrading the transportation system of the City of Coventry and lowering the carbon emissions [29]. The vehicle under development follows a “right material in the right place” strategy adopted from the design of automotive vehicle. Figure 2(a) shows an exploded view of the main components design of the rail vehicle. The prototype design includes a steel bottom chassis and side module, an aluminium roof structure and composite nose mould to improve the stiffness of the vehicle from the safety perspective. However, in order to further reduce the weight to improve the driving performance and efficiency, the composite bottom chassis was proposed with an expect of weight saving of 33.5% (from 922.3 kg to 613.5 kg). Moreover, through the optimisation of the efficiency of energy harvesting, composite bottom chassis is also ideal due to a higher stress distributed with integration of piezoelectric energy harvesters.

This paper aimed at harvesting energy from a multifunctional MFC-embedded composite chassis of a simplified rail vehicle structure (Figure 2(b)), under the representative operational vibration data measured in a rail cabin. The design of the pattern and location of the integrated MFCs within composite chassis was determined by a parametric finite element (FE) study. To meet the actual power demanding of sensors and wireless nodes, the harvested energy was optimised and managed by designing the various rectified circuits strategies. The recoverable rectified power from the chassis vibration was predicted with optimal energy saved compared to other rectification circuit designs. The feasibility of using the harvested energy to sustainably power the smart microsystems was assessed by referring to the power consumptions of such functional components. Figure 3 summarise the schematic of the FE model setup and the power prediction system discussed in this paper.



(a) Exploded view of the main components in the vehicle



(b) Simplified vehicle structure studied in this paper

Figure 2. (a) Exploded view of the main components in the rail vehicle; (b) multi-material design of a simplified light rail vehicle structure. Units in mm. The vehicle length, width and height are 11.0, 2.7 and 3.1 m, respectively.

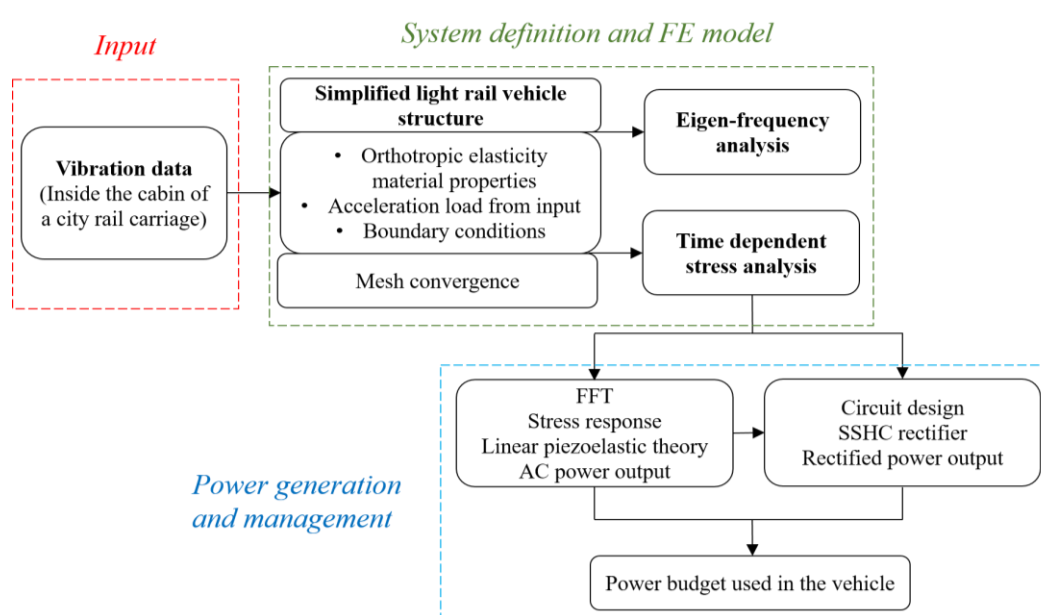


Figure 3. The schematic of the FE model setup and power prediction from the piezoelectric MFC on composite rail chassis when subjected to vibrational data input discussed in this paper.

2. Finite element analysis of the vehicle

2.1. Finite element modal

For balancing the computing efficiency with a full chassis structure, the symmetric model of the vehicle structure was created using Hypermesh code and OptiStruct solver. A shell model was built by extracting the middle surface from the three-dimensional geometry to save computational cost and time. A global element size of 10 mm was confirmed after a parametric study of convergence in the FE solver. The entire chassis structure was primarily joined by rigid connections between different structural components. The definition of boundary conditions of the chassis is illustrated in Figure 4(a): the displacement and rotations of the bogie mount central was restricted as the bogie structures are attached to the wheel and stay stable on the track. Multi-point constraint was used to link all the nodes at the middle section to a built independent node and an x -symmetric boundary condition was employed. The time-dependent accelerations were input to the built independent node and the deformations were expected to be transferred to the entire chassis.

The steel and aluminium structural components were modelled using isotropic natures, with the material properties shown in Table 1. The composite bottom chassis was made from RC200T woven fabric CFRP, with the orthotropic material properties obtained from [28] (also shown in Table 1). An Eigenfrequency study of the half chassis structure was firstly performed and the analysis revealed the natural frequency at 6.018 Hz (1st bending mode, see Figure 4(b)) and 6.763 Hz (1st torsional mode, see Figure 4(c)), with higher resonant modes summarised in Table 2. Time dependent transient response analysis was carried out to determine time-varying dynamic responses of the structure under the given time-dependent acceleration.

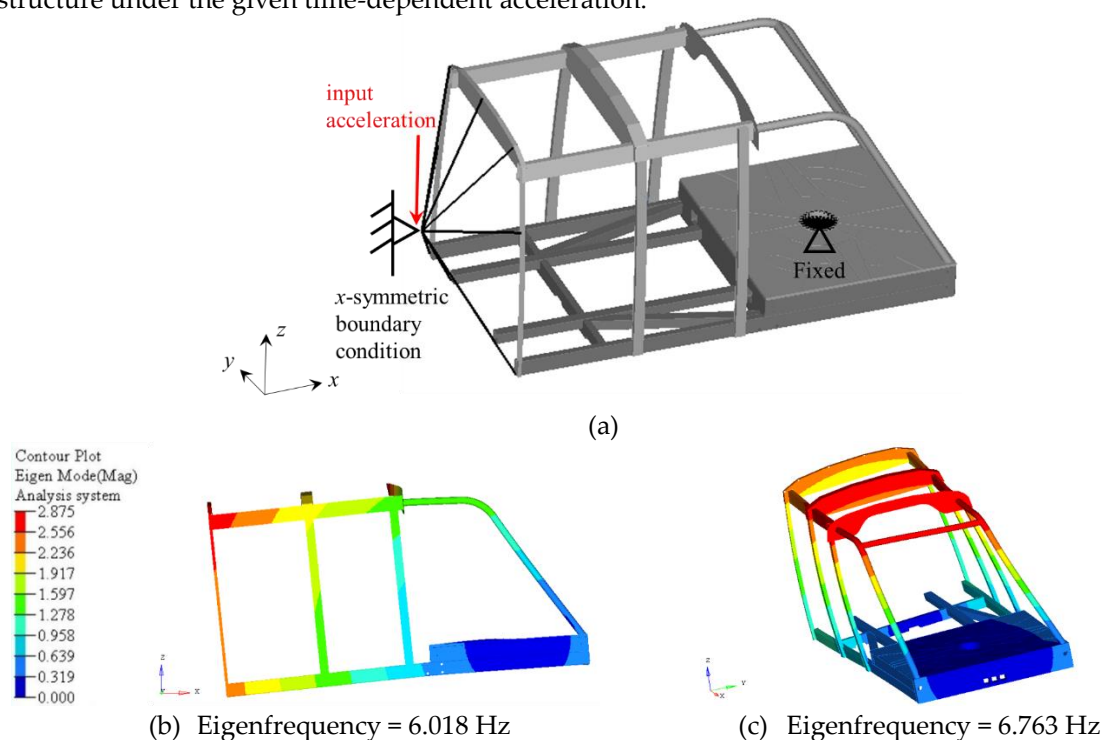


Figure 4. (a) Boundary conditions of the FE model of the vehicle, (b) 1st bending mode (6.018 Hz) and (c) 1st torsional mode (6.763 Hz) of the vehicle.

Table 1. Properties of the materials used in the vehicle structure (material breakdown in Figure 2(b)).

	Elastic modulus (GPa)	Poisson's ratio	Density (kg/m ³)
Steel	210	0.29	7850
Aluminium	69	0.3	2700

CFRP (RC200T) [28]	$E_x = 59.45, E_y = 60.30, E_z = 3.90$ $G_{xy} = 62.90, G_{yz} = 1.50, G_{xz} = 62.35$	$\nu_{xy} = 0.3$ $\nu_{yz} = 0.4$ $\nu_{xz} = 0.3$	1800
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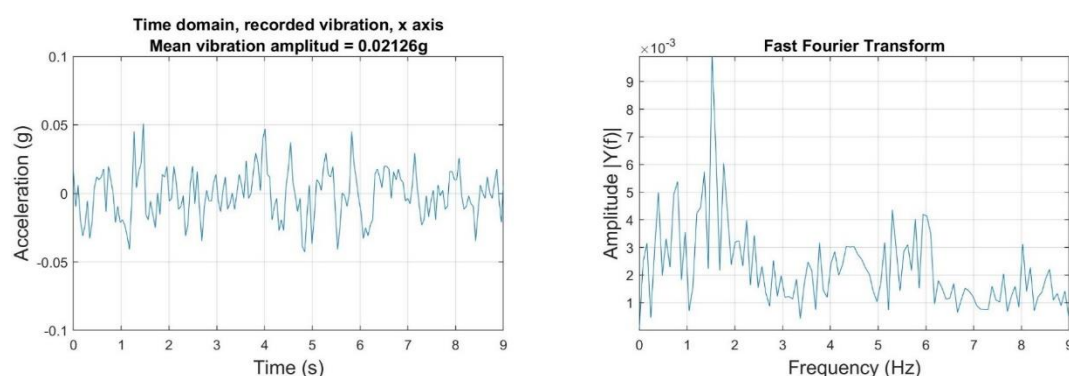
Table 2. Comparison of resonant frequencies for various modes of the vehicle.

Mode	Freq. (Hz)
1 st bending (Figure 4(b))	6.018
2 nd bending	19.935
1 st torsional (Figure 4(c))	6.763
2 nd torsional	14.407
3 rd torsional	21.921
1 st lateral	23.839

2.2. Vibration data analysis

Vibration data was measured directly from a representative environment inside the cabin of a city rail carriage using 3 axis Gulf Coast Data Concepts (GCDC) MEMS accelerometer data loggers with a sample rate of 400 Hz to 800 Hz [30] and has been published in [28]. The total period of the selected data covers approximately 9 s. The axes were defined identical to the coordinate shown in Figure 4(a): x-axis is along the vehicle, y-axis is across the vehicle, and z-axis is vertical through the vehicle. The time domain data were processed and analysed using Fast Fourier Transform (FFT) in MATLAB, as shown in Figure 5. X-axis vibration (mean amplitude was 0.02126 g) contained an evident frequency peak at 1.53 Hz, followed by harmonics at approximately 6 Hz. Y-axis (mean amplitude was 0.01205 g) was more broadband, with a few harmonics at different frequencies. Z-axis vibration (mean amplitude was 0.03007 g) experienced peaks at 1.28 Hz, with a flat active frequency range covering up to 10 Hz. All of the accelerations from the three axes contribute to the movement of the vehicle. It should be noted that the vibration data in the three axes depends on many factors, i.e., the health condition of the vehicle, the track roughness. These acceleration data were used as excitation inputs for the FE model.

It should be noted that the natural frequency of the prototype structure at 6.018 Hz does not match with the first active frequency peak of the three axes vibration data, therefore, the power response was primarily non-resonant for the unmatched case.



(a) X axis

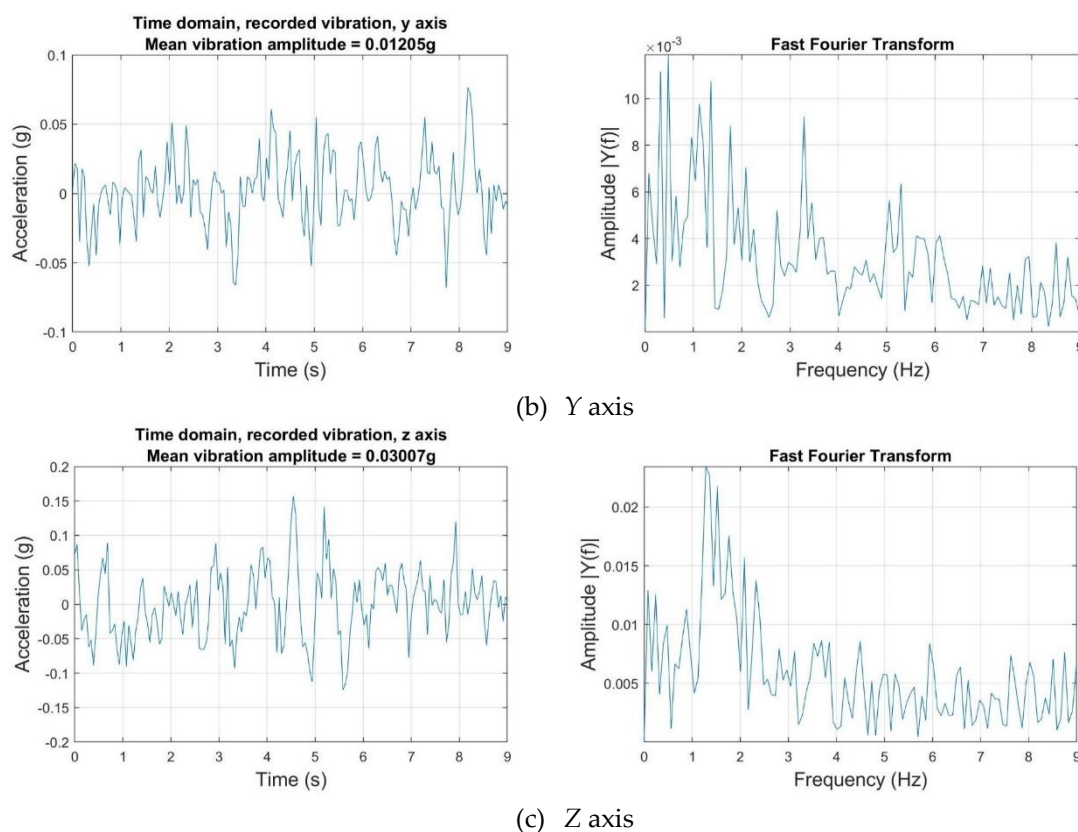


Figure 5. Representative environment vibrations for three axes of train cabin interior, including time domain vibration data and FFT analysis.

2.3. Stress responses used for power prediction

The aim at obtaining the stress responses in this section is used as input for power prediction. Apparently, the stresses on the half chassis structure varies with the time-dependent accelerations. For example, the displacements and von Mises stress responses under three axes accelerations at randomly selected 2.016 s are shown in Figure 6. The chassis behaves in lateral and bending mode under Y and Z-axis accelerations, respectively, with a maximum displacement of 2.43 mm and 14.23 mm at the middle of the chassis. Under X-axis acceleration, the chassis structure performs in primarily longitudinal bending deformation, with the nose structure deforming a maximum of 3.13 mm. Considering at the stress distributions under three axes, stress concentrates at the lower chassis connection points (red circle in Figure 6) and around the bogie mount central (yellow box in Figure 6). A larger stress can also be observed on the chassis beams when Z-axis acceleration is employed due to the bending deformation.

Figure 7 indicates the relationship of von Mises stress vs. time of two elements located at the highest stressed lower chassis and bogie mount central. The signs of the stresses are defined in alignment with the directions of the displacements according to the local axes. The stresses at the two locations peak at approximately 100 MPa, respectively at around 8.5 s and 3.5 s, which is much smaller than the tensile strength of the composite materials (662 MPa [31]). It can be seen that the vibration at the bogie mount fluctuates more than that at the lower chassis indicating a less stable design.

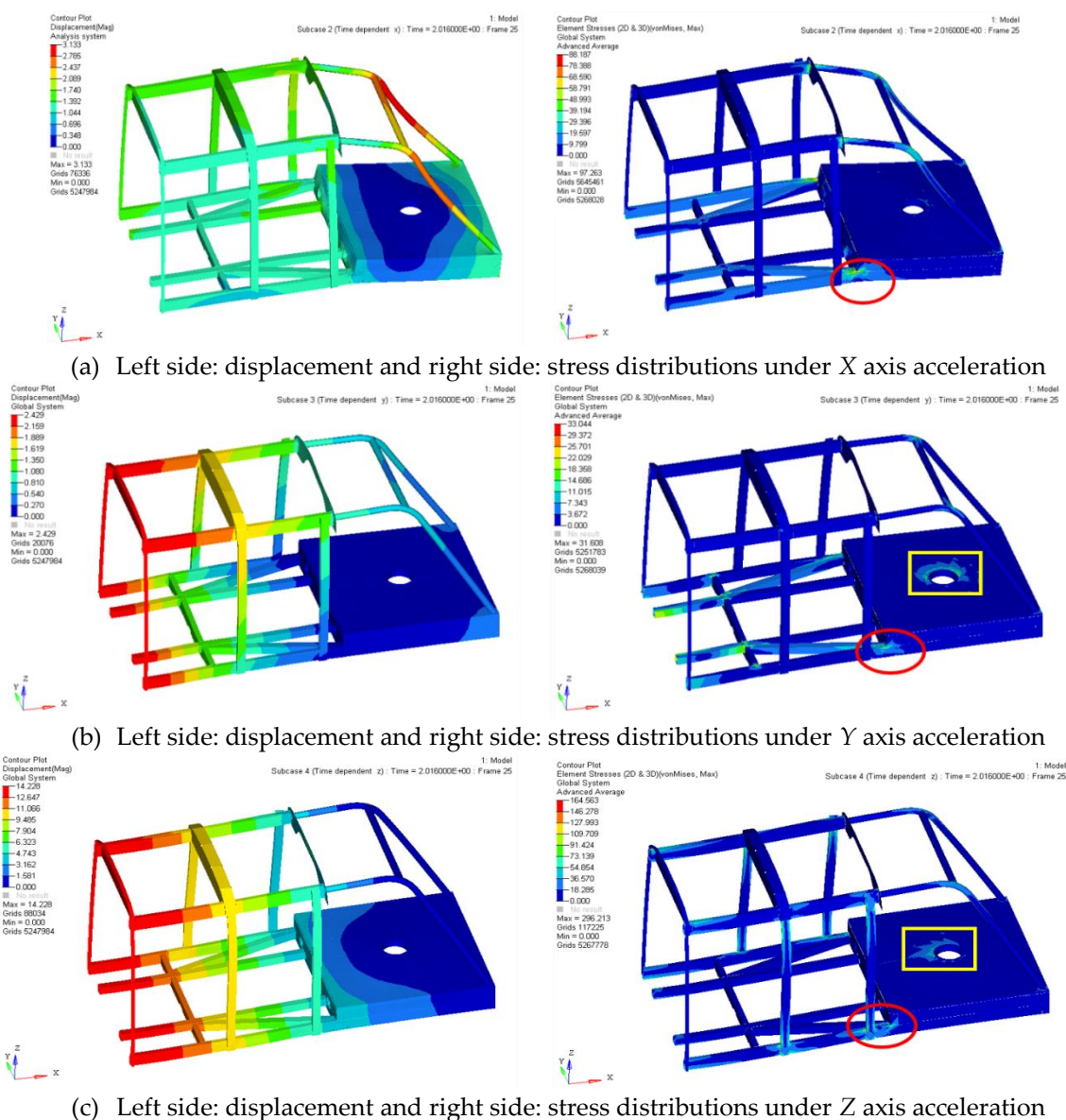


Figure 6. Left side: displacement and right side: stress distributions of the half chassis model under (a) X-axis (Scale factor=100), (b) Y-axis (Scale factor=100) and (c) Z-axis (Scale factor=50) accelerations at 2.016 s; red and yellow box circles the high stress regions at lower chassis connection and bogie mount, respectively.

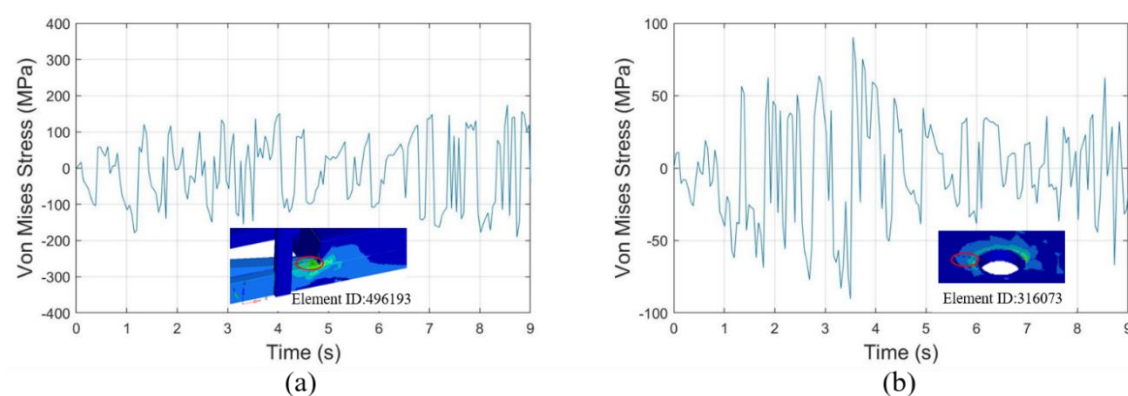


Figure 7. Von Mises stresses vs. time plots of (a) lower chassis connecton, and (b) bogie mount central.

3. Power generation and Management

3.1. AC power prediction using MFC piezoelectric material

The embedded MFC-P2 transducers with designed shape of geometry and dimensions from [32] can be used as the energy harvester. The MFCs were modelled as orthotropic materials using the mechanical properties presented in Table 3, with E_1 and E_2 aligned to the rod and electrode directions, respectively. The piezoelectric and dielectric properties of the MFC are shown in Table 4. In accordance with the time-varying stress distributions in the chassis structure obtained from FE analysis considering the aim to harvest highest power, eight MFC location possibilities (as shown in Figure 8(b)) were evaluated which cover the stress concentration areas and high stress regions. MFC 1 to MFC 4 are designed in rectangular geometry of $100 \times 50 \times 0.3 \text{ mm}^3$ and MFC 5 (same as MFC 6) to MFC 7 (same as MFC 8) are designed in triangular shape with an area domain of 13488.2 mm^3 and 17789.3 mm^3 to fit the geometry of the bogie mount structures.

Table 3. Mechanical properties of MFC [32], E_x and E_y are elastic modulus in the rod and electrode directions, respectively.

E_x (GPa)	E_y (GPa)	G_{xy} (GPa)	ν_{xy}	Density (kg/m ³)
30.34	15.86	5.52	0.31	5400

Table 4. Piezoelectric and dielectric properties of MFC [32].

Charge constant d_{31} (pC/N)	-170
Charge constant d_{33} (pC/N)	400
Capacitance per unit area C_p (nF/cm ²)	7.8
Dielectric permittivity ϵ_p	0.15

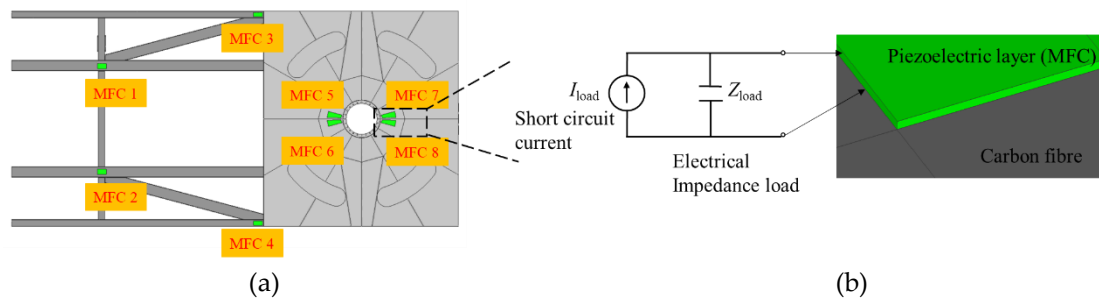


Figure 8. (a) The location possibilities of the MFC transducers on carbon fiber chassis structure, (b) the magnitude of the MFC transducer used to generate electrical power based on an electrical load, Z_{load} .

The time-varying stress responses from the MFC piezoelectric materials was calculated from the time dependent analysis of the global vehicle FE model. Typically, the MFC used in the chassis is ideally suited for vibration energy harvesting even in higher modes, as the opposing stress regions across the single MFC element which might result in partial charge cancellation has not been observed from the FE simulation. This is because the deformation in the MFC region is comparatively small and consistent compared to the large deformation of the entire vehicle. When used as energy harvester, the piezoelectric material can work in d_{31} or d_{33} mode depending on the poling direction and the stress direction. It is typical that the d_{31} mode is usually seen in piezoelectric films, where the electric field is perpendicular to the direction of mechanical strain; d_{33} mode appears as piezoelectric stacks where both electric field and strain are in the poling direction. As charge constant, d , is defined as the short circuit charge density per applied mechanical stress, the generated short circuit charge and current can be summarised by equations (1) and (2) [28],

$$Q_{sc}(t) = d_{31} \sigma_{av}(t) \int_A dA \quad (1)$$

$$I_{sc}(t) = \omega(t) d_{31} \sigma_{av}(t) \int_A dA \quad (2)$$

where Q_{sc} is the short circuit electrical charge; I_{sc} is the short circuit current; σ_{av} is the average stress experienced by the piezoelectric domain and A is the active area of the piezoelectric domain; ω is the frequency where the piezoelectric transducer excites, FFT was carried out on the time domain response from the FE simulation in order to assess the frequency characteristics.

For a given electrical impedance load Z_{load} , the current generated across the load, $I_{load}(t)$ is given by equation (3). To maximise power output, the impedance matching is needed between Z_{load} and Z_i .

For short circuit, $Z_{load} = 0$, the factor $\frac{Z_i}{\sqrt{Z_i^2 + Z_{load}^2}} = 1$. As $Z_{load} \rightarrow \infty$, $\frac{Z_i}{\sqrt{Z_i^2 + Z_{load}^2}} \rightarrow 0$. Therefore the

generated power across a matched impedance load, P_m can be calculated using the following equations:

$$I_{load}(t) = \frac{I_{sc}^2(t) Z_i}{\sqrt{Z_i^2 + Z_{load}^2}} \quad (3)$$

$$Z_{load}(t) = Z_i(t) = \frac{1}{\omega(t) C_p} \quad (4)$$

$$P_m(t) = I_{load}^2(t) Z_{load} \quad (5)$$

where C_p is the capacitance of the piezoelectric material.

With the above-mentioned equations (1)-(5), the power output from each MFC piezoelectric material as well as the total power output were calculated and plotted in Figure 9. The total mean power output from 8 MFCs is 28.34 mW and the peak harvested power during the analysed time period exceeding 100 mW. However, this calculated power is unstable AC power, which is not suitable to transmit, store and distribute efficiently. For the purpose of a better conversion and management of the harvested energy, conditioned DC power are always adopted.

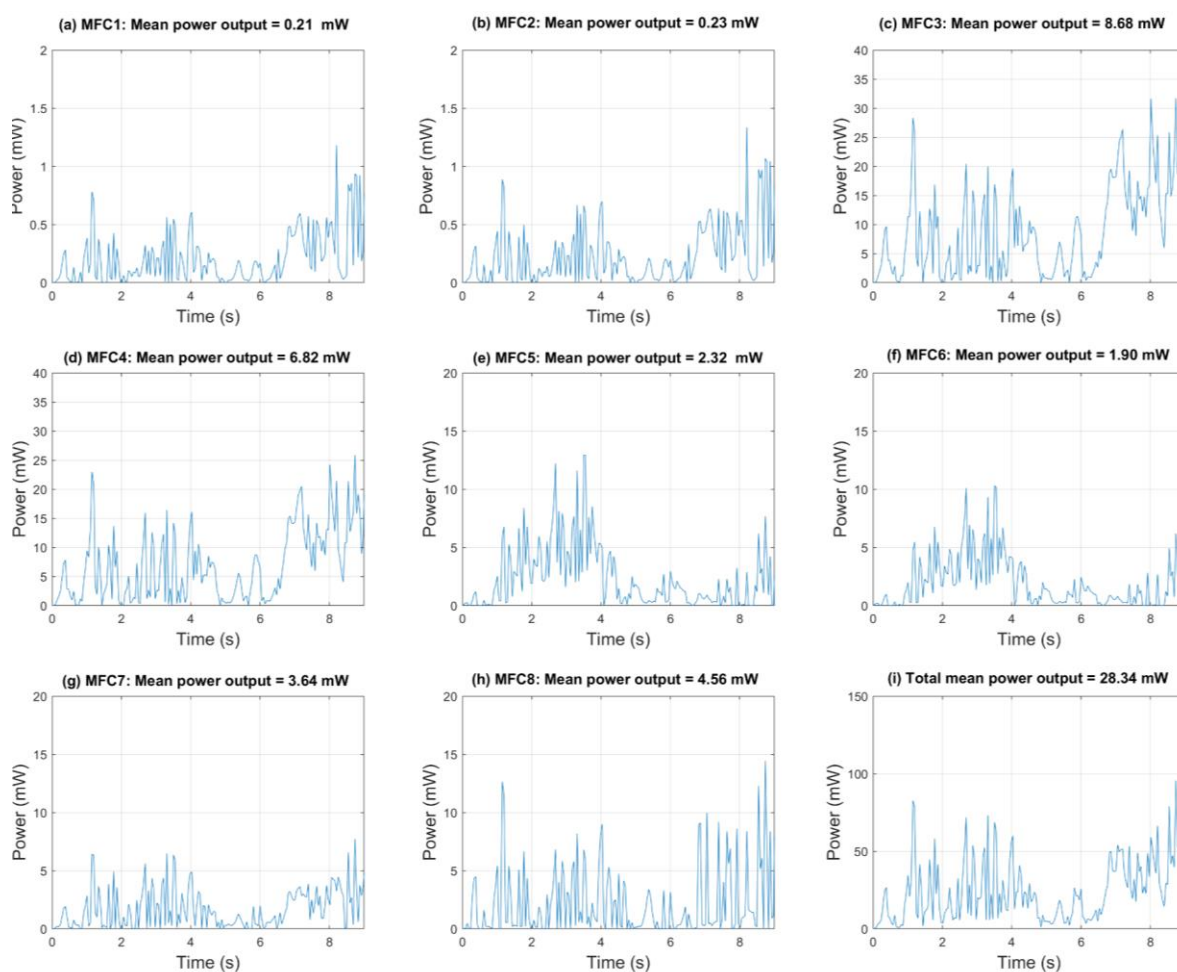


Figure 9. Power output calculated from 8 MFC piezoelectric materials.

3.2. Rectified power prediction

Since the harvested power is to be used to power electronic devices, which typically require DC power supplies, rectification circuits are needed to provide usable DC power for potential loads. This section provides the rectified output power estimation and analysis using both passive and popular active rectification circuits. Full-bridge rectifiers (FBR) are widely used due to simplicity and stability; however, the poor output power of FBRs hindered the development of active rectification circuits in the past decade [33]. The synchronised switch harvesting (SSH) architecture is one of the most promising rectification systems to provide high energy efficiency for piezoelectric energy harvesting [34]. In this section, the output power from a passive FBR, switch-only (SO) and SSH on capacitors (SSHC) was simulated and analysed to show the peak DC output of the proposed energy harvesting system.

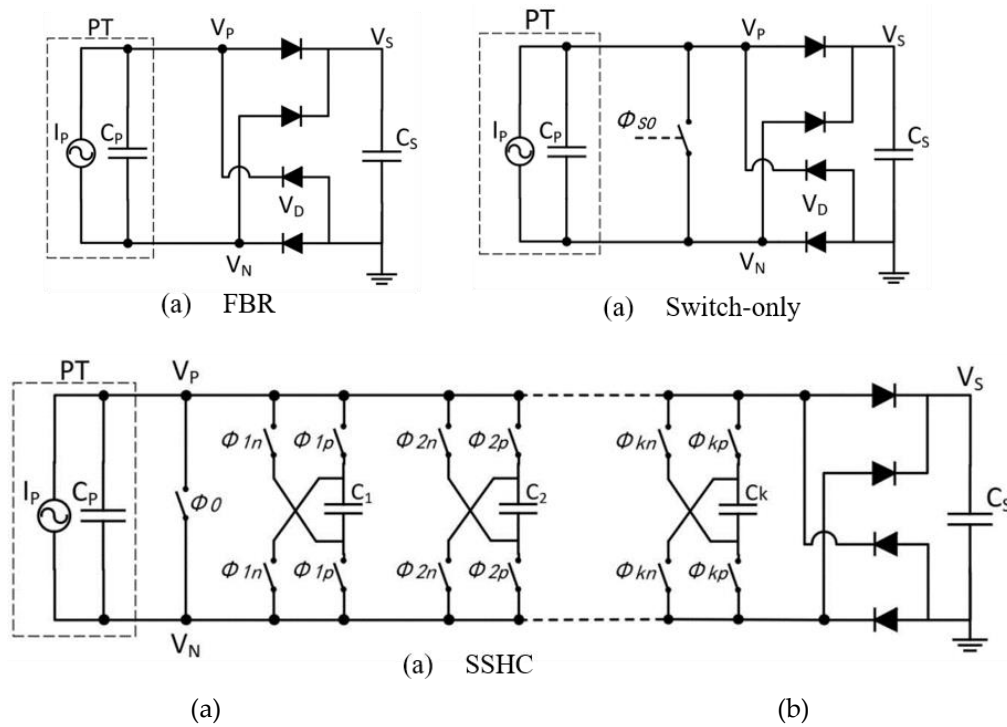


Figure 10. (a) Circuit diagram of an FBR, (b) a SO rectifier and (c) an SSHC rectifier.

The circuit diagrams of an FBR, a SO rectifier and an SSHC rectifier are shown in Figure 8. In the diagrams, the piezoelectric transducer (PT) has been modelled as a current source (I_P) in parallel with its inherent capacitor (C_P). In these three rectifiers, only the FBR is a passive rectifier using 4 passive diodes. The SO and SSHC rectifiers are active rectifiers requiring additional circuit designs to generate the control signals to drive the switches. The circuit implementations of the SSHC rectifier have been detailed in [34]. The number k represents the number of capacitor stages to perform as a k -stage SSHC rectifier. The SO rectifier is a simplified SSHC rectifier with the ϕ_0 switch only by removing all the following capacitor stages. Hence, the SO rectifier can be also regarded as a zero-stage SSHC rectifier.

The rectified output power of all the eight MFC elements when using different rectification circuits was simulated and is shown in Figure 11. The simulations were based on the current sources calculated from the linear piezoelectric theory with the average stress outputs obtained from finite element analysis. The horizontal axis is the output voltage of the rectifier, which is also the voltage across the output capacitor connected at each rectification circuit, V_S , as shown in Figure 10. For the SSHC rectifier, different numbers of employed capacitors are simulated for various output power values with different performance levels. The more capacitors that are employed, the higher the peak output power that is achieved. However, more capacitors in SSHC rectifiers also result in more complicated control circuits, larger system sizes and higher optimal output voltage levels to achieve the peak power. The simulations were performed for V_S values ranging up to 300 V. The peak output power of each rectifier and the corresponding optimal output power are summarised in Table 5. From this table, it can be found that when using a passive FBR, the peak rectified power is around 21.2 mW from all the 8 MFC elements. When an 8-stage SSHC rectifier is employed, the peak rectified power achieves 181.9 mW, which is more than 8 times higher compared to a passive FBR. In order to achieve this high output power, the output voltage, V_S , of the SSHC rectifier needs to be maintained at around 300 V. Since this optimal voltage is usually higher than supply voltages for most low-power

loads, an efficiency DC-DC converter and a voltage regulator are typically required to power the load electronics.

It is worthwhile analysing the power contributions from different MFC elements for future design optimisations. The peak rectified output power values from individual MFC elements are shown in Table 6. It can be clearly seen that the MFC 3 and MFC 4 contribute more than 90% of the total rectified power. This is because MFC 3 and MFC 4 are mechanically located at stress concentration regions (welding connections within the adjacent host structures), inducing a high stress output and therefore the highest power output.

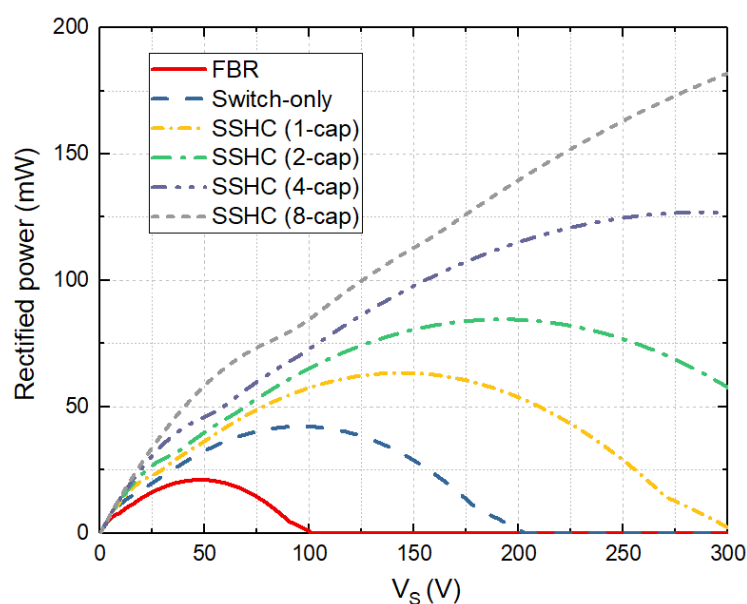


Figure 11. Simulated rectified output power using FBR, switch-only (SO) rectifier and SSHC rectifier (with different numbers of capacitor stages) for all the eight MFC elements.

Table 5. Peak rectifier power for each rectification circuit and the corresponding optimal output voltage.

Rectifiers	Peak power (mW)	Optimal VS (V)
FBR	21.2	48
Switch-only	42.3	96
SSHC (1-cap)	63.4	144
SSHC (2-cap)	84.6	192
SSHC (4-cap)	126.9	288
SSHC (8-cap)	181.9	300

Table 6. Peak output power from individual MFC elements and their contributions to the total power.

MFC No.	Peak rectified power (mW)						Percentage (%)
	FBR	Switch-only	SSHC (1-cap)	SSHC (2-cap)	SSHC (4-cap)	SSHC (8-cap)	
1	0.28	0.56	0.84	1.12	1.68	2.79	1.2
2	0.31	0.61	0.92	1.23	1.84	3.06	1.3
3	11.89	23.78	35.67	47.57	71.35	118.92	51.7

4	9.34	18.68	28.01	37.35	56.03	93.38	40.6
5	0.24	0.47	0.71	0.94	1.41	2.36	1.0
6	0.19	0.39	0.58	0.77	1.16	1.94	0.8
7	0.35	0.69	1.04	1.38	2.07	3.46	1.5
8	0.41	0.82	1.22	1.63	2.45	4.08	1.8

4. Discussion on use of power budget

It is clear that the energy harvesting from the vehicle vibration itself is impossible to meet the power requirement of the motors and actuators, as the motive power requirement is more than an order of magnitude higher than what energy harvesting can provide. However, the recoverable power is sufficient to meet the power requirements of sensors, microprocessors and wireless systems which are important to railway infrastructures to regulate maintenance and to ensure safety. In order to study the impact of the recovered power a possible route for the new rail vehicle was analysed. The vehicle speed based on initial route assumptions is shown in Figure 12. The route is defined over a route of 14 km within the City of Coventry, with known locations of seventeen stop stations. The route speed limit is defined according to the standards in the United Kingdom. The entire running time period of one route is approximately 20 mins (1200 s) based on the speed limits.

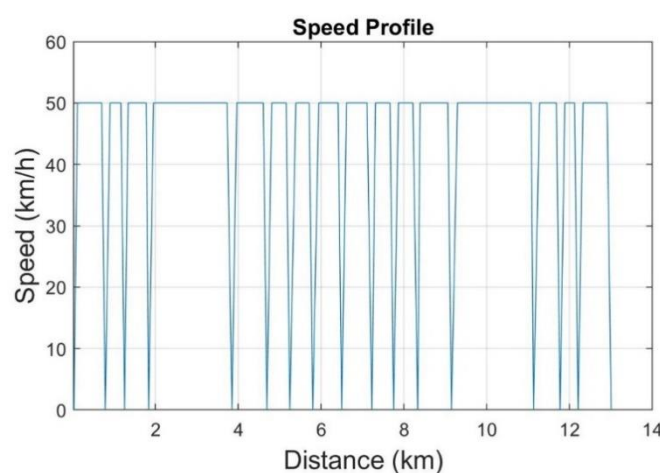


Figure 12. Speed profile of this vehicle vs. distance.

In order to assess the meaningfulness of the calculated recoverable power, the typical power requirements of various functionally sensors, controller and wireless systems are summarised in Table 7. Some of the power consumptions do not need to be in active operation all the time and smart power management can help to reduce the power budget. A power requirement for one journey was estimated to be 153 mW and this could be met by the harvested power from the vehicle vibrations. Table 8 compares different types of rail harvesting sources from the open literature to evaluate the accuracy of the calculated power budget as well as to understand the harvested power contributions from a wide range of sources. Most of the literature investigated energy harvesting from train induced railway track vibrations, such as, Wang et al. [35] and Wang et al. [36] who proposed the use of an electromagnetic generator and piezoelectric transducers embedded in the track to harvest energy from the moving vehicle loads mainly via experimental testing. Cleante et al. [37] analytically investigated the amount of harvested energy induced by a passing train at various speeds using a trackside energy harvester. Tehrani et al. [38] analytically calculated a single spring-mass-damper system used as the energy harvester with the measured acceleration from a train cabin. Although these works contain basic analytical modelling, they lack consideration of sprung mass vibrations and the electronic network between various energy harvesters. Wheelwright et al. [39] established a

vibration-based condition system product for the monitoring, management and maintenance of wheelsets of rolling stock to prevent failures. In terms of the railway station network, Jiang et al. [40] built electronics storage schemes for regenerative energy from railway stations to reduce the operating costs and improve the operational safety of railways. However for the first time, this work takes account of energy harvesting from sprung mass vibrations in the train chassis using both finite element modelling of prototype design and electronics simulation optimisation, which is more representative of the realistic scenarios.

Table 7. Estimated power budget of the sensor platform with the application of the route assumption of this vehicle.

Power budget item	Power (mW)	Active in period (%)	Active time in one route cycle (s)	Power in one route cycle (mW)
MEMS 9 DOF motion sensor + MPU [41] ×2 units	0.05	100%	1200	1
Inclinometers [42] ×2 units	56.25	100%	1200	112.50
Distance sensors [43] ×2 units	13.95	100%	1200	27.90
Microprocessor unit (MPU) (active mode [44]) ×2 units	0.36	100%	1200	0.72
Bluetooth 5 + RF chip (transceiver mode [45]) ×2 units	27	20%	240	10.80
Bluetooth 5 + RF chip (sleep mode, clock [45]) ×2 units	0.045	80%	960	0.08
Sum				153.00

Table 8. Different types of energy harvested in the rail from the literatures.

Type of rail harvesting	Energy harvest	Methodology	Comments
Train induced track vibration	2-4 volts	Experiments	For 6.35mm track displacement input, from Wang et al. [35]
	0.02 mW - 0.2 mW	Experiments Analytical modelling	For slack-type and patch-type piezoelectric transducers, from Wang et al. [36]
	100.3 mW - 157.1 mW	Analytical modelling	With passing train speed from 190 to 200 km/h, from Cleante et al. [37]
Electrification of railway stations	541.6 kW	Electronics simulation	Jiang et al. [40]
Unsprung mass vibration	21.4 mW	Analytical modelling	Ghandchi Tehrani et al. [38]
	1-5 wheel health index	Experiments	Wheelwright et al. [39]
Sprung mass vibration	21.2 mW - 181.9 mW	Finite element modelling Electronics simulation	This work

5. Conclusions

This paper presented the energy generation from a multifunctional MFC-embedded composite chassis of a rail structure. The rectification circuits are designed to help the optimisation and power management for harvested energy under the real-world vibration data measured in a cabin of a rail vehicle. A finite element model was built to numerically predict the time dependent stress responses

using representative three axis acceleration data. Eight locations were therefore determined at the bottom chassis for integrating the piezoelectric energy harvesters. The analytical model was developed to explain the energy harvesting mechanisms. The rectification circuit design of the various passive and active rectification systems were proposed to design to help the optimisation and management of harvested energy. The results showed that a peak of 181.9 mW DC electric power was approximately recovered when an eight-stage SSHC rectifier was employed. Compared to the other designs and case without such circuit design optimisation, it generates high output power compared to the AC power, FBR and the switch-only rectifier which makes it suitable to meet the required power budget. The power level achieved by harvesting operational vibration was considered to be sufficiently and continuously sustain a simple sensor service platform, considering a hypothetical average power budget consumption of 153 mW. The novel optimisation using rectification circuits for improving the efficiency of energy harvesting has rarely been reported and the success of maximising the energy harvested in this paper offers a significant opportunity to enable micro-watt power scavenging from ambient vibrations towards the realistic applications.

In the near future, a prototype of the composite chassis of rail vehicle will be fabricated with integration of energy harvesters based on the current design and optimised rectification circuits. Experimental testing under mechanical vibrations with the various operational and environmental conditions will be performed to validate this work which will point a route for further exploitation not only in the rail industry, but also the automotive, offshore wind energy and aerospace sectors.

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Abbreviations

The following abbreviations are used in this manuscript:

CFRP	carbon fibre reinforced polymer
FBR	full-bridge rectifiers
FEA	finite element analysis
MFC	micro fibre composites
SO	switch-only
SSHC	synchronized switch harvesting capacitors

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